TASI 2012

The Infrared

Confinement

Hadronization

Underlying Event & Soft QCD interactions

Disclaimer

Focus on ideas, make you think about the physics

P. Skands (CERN)

From Partons to Pions

Here's a fast parton



From Partons to Pions

Here's a fast parton



How about I just call it a hadron?

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QCD

From Partons to Pions

Here's a fast parton



How about I just call it a hadron?

 \rightarrow "Local Parton-Hadron Duality"

Parton → Hadrons?

Parton Hadron Duality

Universal fragmentation of a parton into hadrons



*LPHD = Local Parton Hadron Duality

QCD

Parton → Hadrons?

Parton Hadron Duality

Universal fragmentation of a parton into hadrons



But ...

- The point of confinement is that partons are <u>colored</u>
- Hadronization = the process of color <u>neutralization</u>

I.e, the one question NOT addressed by LPHD or I.F.

→ Unphysical to think about independent fragmentation of individual partons

*LPHD = Local Parton Hadron Duality

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Color Neutralization

A physical hadronization model

Should involve at least TWO partons, with opposite color charges (e.g., **R** and **anti-R**)



Strong "confining" field emerges between the two charges when their separation $> \sim 1 \text{ fm}$

Lattice QCD: Potential between a quark and an antiquark as function of distance, R



 \mathbf{V}

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 \mathbf{V}

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Lattice QCD: Potential between a quark and an antiquark as function of distance, R



Long Distances ~ Linear Confinement





QCD Lecture

Lattice QCD: Potential between a quark and an antiquark as function of distance, R

"Quenched" Lattice QCD K(R) 0.9linear par 0.8 total 0.7 Short Distances ~ pQCD 0.6 Coulomb part 0.5 0.4 ^D $V(R) = V_{p} + K R - e/R + f/R^{2}$ Partons 0.3 16 12 20 8 24R

Long Distances ~ Linear Confinement





 $F(r) \approx \text{const} = \kappa \approx 1 \text{ GeV}/\text{fm} \iff V(r) \approx \kappa r$

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Long Distances ~ Linear Confinement



Hadrons

Question: What physical system has a linear potential?

 $F(r) \approx \text{const} = \kappa \approx 1 \text{ GeV}/\text{fm} \iff V(r) \approx \kappa r$

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From Partons to Strings



Motivates a model:

- Let color field collapse into a (infinitely) narrow flux tube of uniform energy density $\kappa \sim 1$ GeV / fm
- → Relativistic I+I dimensional worldsheet string

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Hadronization Models

The problem:

Given a set of partons resolved at a scale of ~ I GeV (the perturbative cutoff), need a "mapping" from this set onto a set of on-shell colour-singlet (i.e., confined) hadronic states.

MC models do this in three steps

- Map partons onto continuum of excited hadronic states (called 'strings' or 'clusters')
- 2. Iteratively map strings/clusters onto **discrete set of primary hadrons** (string breaks / cluster splittings / cluster decays)
- 3. Sequential decays into secondary hadrons (e.g., $\rho > \pi \pi$, $\Lambda^0 > n \pi^0$, $\pi^0 > \gamma\gamma$, ...)

Distance Scales ~ 10⁻¹⁵ m = 1 fermi



Between which partons do confining potentials arise?

Set of simple rules for color flow, based on large-N limit

(Never Twice Same Color: true up to $O(1/N_c^2)$)

QCD

Lecture

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Illustrations from: P.Nason & P.S., PDG Review on *MC Event Generators*, 2012 QCD

Lecture

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From Partons to Strings

Illustrations by T. Sjöstrand

Map: • **Quarks** \rightarrow String Endpoints g (<u>**r**</u>b) • **Gluons** → Transverse snapshots of string position Excitations (kinks) • q (<u>r</u>) Strings stretched from q endpoint, via any number of gluons, to qbar endpoint व (<mark>b</mark>

QCD



Coherence of pQCD cascades \rightarrow not much "overlap" between strings \rightarrow planar approx pretty good

(LEP measurements in WW confirm this (at least to order $10\% \sim 1/N_c^2$))

Note: (much) more color getting kicked around in hadron collisions \rightarrow color reconnections important there? ...

For an entire Cascade



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$$\mathcal{P} \propto \exp\left(-\frac{\pi m_{\perp q}^2}{\kappa}\right) = \exp\left(-\frac{\pi p_{\perp q}^2}{\kappa}\right) \exp\left(-\frac{\pi m_q^2}{\kappa}\right)$$

1) common Gaussian p_{\perp} spectrum 2) suppression of heavy quarks $u\overline{u} : d\overline{d} : s\overline{s} : c\overline{c} \approx 1 : 1 : 0.3 : 10^{-11}$ 3) diquark \sim antiquark \Rightarrow simple model for baryon production

> Lecture V

QCD



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Also depends on:

Spins, hadron multiplets, hadronic wave functions, phase space, ...

 \rightarrow (much) more complicated \rightarrow many parameters

 \rightarrow Not calulable, must be constrained by data \rightarrow 'tuning'

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Fragmentation Function



Fragmentation Function



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Left-Right Symmetry

Causality → Left-Right Symmetry

- → Constrains form of fragmentation function!
- → Lund Symmetric Fragmentation Function



$$f(z) \propto \frac{1}{z} (1-z)^a \exp\left(-\frac{b\left(m_h^2 + p_{\perp h}^2\right)}{z}\right)$$



Lecture V

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Iterative String Breaks

Causality \rightarrow May iterate from outside-in



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Alternative: The Cluster Model

"Preconfinement"



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 10^{2}

 10^{3}

Alternative: The Cluster Model



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Alternative: The Cluster Model



Strings and Clusters



Small strings \rightarrow clusters. Large clusters \rightarrow strings

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String Hadronization

Main IR Parameters

Longitudinal FF = f(z)



pT in string breaks



Lund Symmetric Fragmentation Function

The a and b parameters

Scale of string breaking process

<pt> in string breaks



Meson Multiplets



Strangeness suppression, Vector/Pseudoscalar, η , η' , ...

Baryon Multiplets

Baryons

Mesons



Diquarks, Decuplet vs Octet, popcorn, junctions, ... ?

QCD
Fragmentation Tuning

(example)



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Hadron Collisions



FIG. 3. Charged-multiplicity distribution at 540 GeV, UA5 results (Ref. 32) vs simple models: dashed low p_T only, full including hard scatterings, dash-dotted also including initial- and final-state radiation.

Sjöstrand & v. Zijl, Phys.Rev.D36(1987)2019



Hadron Collisions



Do not be scared of the failure of physical models Usually points to more interesting physics



FIG. 3. Charged-multiplicity distribution at 540 GeV, UA5 results (Ref. 32) vs simple models: dashed low p_T only, full including hard scatterings, dash-dotted also including initial- and final-state radiation.

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Hadron Collisions







FIG. 12. Charged-multiplicity distribution at 540 GeV, UA5 results (Ref. 32) vs multiple-interaction model with variable impact parameter: solid line, double-Gaussian matter distribution; dashed line, with fix impact parameter [i.e., $\tilde{O}_0(b)$].

Sjöstrand & v. Zijl, Phys.Rev.D36(1987)2019

Soft-inclusive QCD



What is Underlying Event ?



Useful variable in hadron collisions: **Rapidity**

Designed to be additive under Lorentz
Boosts along beam (z) direction
$$y = \frac{1}{2} \ln \left(\frac{E + p_z}{E - p_z} \right)$$

$$y \to -\infty$$
 for $p_z \to -E$ $y \to 0$ for $p_z \to 0$ $y \to \infty$ for $p_z \to E$

Illustrations by T. Sjöstrand

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Designed to be additive under Lorentz Boosts along beam (z) direction

$$y = \frac{1}{2} \ln \left(\frac{E + p_z}{E - p_z} \right)$$

Homework: Check how y transforms under Lorentz boost along z

$$y \to -\infty$$
 for $p_z \to -E$ $y \to 0$ for $p_z \to 0$

 $y \to \infty$ for $p_z \to E$

Illustrations by T. Sjöstrand

QCD

Twisted Stuff

Factorization: Subdivide Calculation



Multiple Parton Interactions go beyond existing theorems

- → perturbative short-distance physics in Underlying Event
- \rightarrow Need to generalize factorization to MPI

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Twisted Stuff

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Multiple Interactions

= Allow several parton-parton interactions per hadron-hadron collision. Requires extended factorization ansatz.



Earliest MC model ("old" PYTHIA 6 model) Sjöstrand, van Zijl PRD36 (1987) 2019



Lesson from bremsstrahlung in pQCD: divergences → fixed-order breaks down Perturbation theory still ok, with resummation <u>(unitarity)</u>

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How many?

Naively $\langle n_{2\to 2}(p_{\perp \min}) \rangle = \frac{\sigma_{2\to 2}(p_{\perp \min})}{\sigma_{tot}}$ Interactions independent (naive factorization) \rightarrow Poisson



$$\mathcal{P}_n = rac{\langle n
angle^n}{n!} e^{-\langle n
angle}$$

Real Life

Momentum conservation suppresses high-n tail + physical correlations → not simple product

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1: A Simple Model

The minimal model incorporating single-parton factorization, perturbative unitarity, and energy-and-momentum conservation

$$\sigma_{2\to 2}(p_{\perp \min}) = \langle n \rangle(p_{\perp \min}) \sigma_{\text{tot}}$$

Parton-Parton Cross Section

Hadron-Hadron Cross Section

I. Choose *p*_{*T*min} cutoff

= main tuning parameter

- 2. Interpret $< n > (p_{T\min})$ as mean of Poisson distribution Equivalent to assuming all parton-parton interactions equivalent and independent ~ each take an instantaneous "snapshot" of the proton
- 3. Generate *n* parton-parton interactions (pQCD $2\rightarrow 2$) Veto if total beam momentum exceeded \rightarrow overall (E,p) cons
- 4. Add impact-parameter dependence $\rightarrow \langle n \rangle = \langle n \rangle(b)$ Assume factorization of transverse and longitudinal d.o.f., \rightarrow PDFs : f(x,b) = f(x)g(b) b distribution \propto EM form factor \rightarrow JIMMY model Butterworth, Forshaw, Seymour Z.Phys. C72 (1996) 637 Constant of proportionality = second main tuning parameter
- 5. Add separate class of "soft" (zero-pt) interactions representing interactions with $p_T < p_{T\min}$ and require $\sigma_{soft} + \sigma_{hard} = \sigma_{tot}$ \rightarrow Herwig++ model Bähr et al, arXiv:0905.4671

(2: Interleaved Evolution)

Sjöstrand, P.S., JHEP 0403 (2004) 053; EPJ C39 (2005) 129

Add exclusivity progressively by evolving everything downwards. p_\perp $\frac{\mathrm{d}\mathcal{P}}{\mathrm{d}p_{\perp}} =$ $p_{\perp \max}$ p_{\perp}^2 $\left(\frac{\mathrm{d}\mathcal{P}_{\mathrm{MI}}}{\mathrm{d}p_{\mathrm{I}}} + \sum \frac{\mathrm{d}\mathcal{P}_{\mathrm{ISR}}}{\mathrm{d}p_{\mathrm{I}}} + \sum \frac{\mathrm{d}\mathcal{P}_{\mathrm{JI}}}{\mathrm{d}p_{\mathrm{I}}}\right) \times$ Fixed order (B)SM evolution $2 \rightarrow 2$ $p_{\perp 1}$ matrix elements Parton Showers $\exp\left(-\int_{p_{\perp}}^{p_{\perp}i-1}\left(\frac{\mathrm{d}\mathcal{P}_{\mathrm{MI}}}{\mathrm{d}p'_{\perp}}+\sum\frac{\mathrm{d}\mathcal{P}_{\mathrm{ISR}}}{\mathrm{d}p'_{\perp}}+\sum\frac{\mathrm{d}\mathcal{P}_{\mathrm{JI}}}{\mathrm{d}p'_{\perp}}\right)\mathrm{d}p'_{\perp}\right)$ ISR (matched to 00000 $p_{\perp 1}$ further Matrix interleaved Elements) mult. int. → Underlying Event multiparton ISR (note: interactions correllated in colour: 00000 PDFs derived from sum rules hadronization not independent) interleaved 00000 mult. int. \sim "Finegraining" **ISR** 00000 00000 00000 perturbative "intertwining"? interleaved \rightarrow correlations between - - - - - - -Intertwined? mult int. $p_{\perp 4}$ all perturbative activity ISR 00000 Beam remnants at successively smaller scales Fermi motion / $p_{\perp \min}$ primordial k_T int. number 2 3



Color Space in hadron collisions



Color Connections

Each MPI (or cut Pomeron) exchanges color between the beams

The colour flow determines the hadronizing string topology

- Each MPI, even when soft, is a color spark
- Final distributions <u>crucially</u> depend on color space



Different models

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Different models

Color Connections

Better theory models needed



Color Reconnections?

E.g.,

Generalized Area Law (Rathsman: Phys. Lett. B452 (1999) 364) Color Annealing (P.S., Wicke: Eur. Phys. J. C52 (2007) 133)

Rapidity

Better theory models needed

Do the systems really form and hadronize independently?

Multiplicity × NMPI

QCD

Main IR Parameters

Number of MPI



Pedestal Rise



Strings per Interaction



QCD

Main IR Parameters

Number of MPI



Infrared Regularization scale for the QCD $2 \rightarrow 2$ (Rutherford) scattering used for multiple parton interactions (often called p_{T0}) \rightarrow size of overall activity

Pedestal Rise



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QCD

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Proton transverse mass distribution \rightarrow **difference betwen central (active) vs peripheral (less active) collisions**

Strings per Interaction



QCD Lecture

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Color correlations between multiple-parton-interaction systems \rightarrow shorter or longer strings \rightarrow less or more hadrons per interaction

QCD

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QCD

LHC from 900 to 7000 GeV - ATLAS



Track Density (TRANS)

Sum(pT) Density (TRANS)

Lecture V

QCD

"Toward"

LHC from 900 to 7000 GeV - ATLAS



Track Density (TRANS)

Not Infrared Safe Large Non-factorizable Corrections

Prediction off by $\approx 10\%$

Sum(pT) Density (TRANS)

Lecture

QCD

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Sum(pT) Density (TRANS)

(more) Infrared Safe

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Prediction off by < 10%

QCD

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R. Field: "See, I told you!"

"Toward"

"Away"

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QCD

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Y. Gehrstein: "they have to fudge it again"

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Lecture

"Toward"

LHC from 900 to 7000 GeV - ATLAS



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Truth is in the eye of the beholder:

"Toward"

"Away"

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Lecture

Y. Gehrstein: "they have to fudge it again"

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Summary 1/2

Fixed Order pQCD: Good for jets ~ hard scale

- Beware: hierarchies / multi-scale problems
- → Scale choices become more important and more complicated
- → Enhancements from soft/collinear (conformal) singularities can invalidate fixed-order truncation

Parton Showers: Good for jets << hard scale

- Bootstrapped approximation to infinite-order perturbation theory (resummation)
- Exact in soft/collinear limits. Unpredictive for hard radiation
- Coherence → Angular Ordering or Dipole-Antenna showers

QCD

Summary 2/2

Matching

At tree level (CKKW, MLM) \rightarrow LO for multiple hard jets

At NLO (MC@NLO, POWHEG) → NLO precision for Born

Substantial modeling uncertainties for soft physics. But fortunately ... it's soft.

Hadronization: based on tracing color flow through event. String model based on linear confinement, causality, and tunneling. Cluster model based on preconfinement and phase space.

Underlying Event: based on multiple parton interactions and impact-parameter dependence.

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Thank you

Additional Slides

Large System

Illustrations by T. Sjöstrand



V

Large System

Illustrations by T. Sjöstrand



String breaks causally disconnected

- → can proceed in arbitrary order (left-right, right-left, in-out, ...)
 - \rightarrow constrains possible form of fragmentation function
 - → Justifies iterative ansatz (useful for MC implementation)

QCD
Multi-Parton PDFs





How are the initiators and remnant partons correllated?



- in impact parameter?
- in flavour?
- in x (longitudinal momentum)?
- in k_T (transverse momentum)?
- in colour (→ string topologies!)
- What does the beam remnant look like?
- (How) are the showers correlated / intertwined?

QCD





QCD

Lecture V



Lecture V

QCD



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Lecture



QCD

Lecture



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"Intuitive picture"

