Peter Skands (CERN)


## VINCIA

$$
\text { Peter } S k \text { a } n d s \quad(C E R N)
$$



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PM Perturbative Evolution $2 \operatorname{Re}\left[M_{H}^{(1)} M_{H}^{(0) *}\right]$

Factorization Scale

## VINCIA

$$
\text { Peter } S k \text { a } n d s \quad(C E R N)
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$\left|M_{H}^{(0)}\right|^{2}$
Perturbative Evolution
$2 \operatorname{Re}\left[M_{H}^{(1)} M_{H}^{(0) *}\right]$

Factorization Scale

## VINCIA

$$
\text { Peter } S k \text { a } n d s \text { (CERN) }
$$



## Why?

Jet Substructure

## Underlying Event \& Jet Calibration

Hadronization

Structure of QCD

## Why?

Jet Substructure

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Hadronization

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Structure of QCD

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Hadronization


Structure of QCD


Better control of perturbative part
$\rightarrow$ better constraints on non-perturbative part

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## Jet Substructure



## Hadronization



Better control of perturbative part
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## Underlying Event \& Jet Calibration



## VINCIA

## What is it?

Plug-in to PYTHIA 8 (http://projects.hepforge.org/vincia)

## What does it do?


"Matched Markov antenna showers"
Improved parton showers

+ Re-interprets tree-level matrix elements as $2 \rightarrow n$ antenna functions
+ Extends matching to soft region (no "matching scale")
Extensive (and automated) uncertainty estimates
Systematic variations of shower functions, evolution variables, $\mu_{R}$, etc.
$\rightarrow$ A vector of output weights for each event (central value $=$ unity $=$ unweighted)


## Who is doing it?

GEEKS: Giele, Kosower, Skands + Gehrmann-de-Ridder \& Ritzmann (mass effects), Lopez-Villarejo ("sector showers"), Hartgring \& Laenen (NLO multileg)

## pQCD with Markov Chains

Starting Point: reformulate perturbative series as Markov Chain
~ all-orders parton shower with all-orders matrix-element corrections

For Each "Evolution Step" = increase in parton multiplicity (on-shell)
Cover all of phase space with (large) trial overestimate = "approximate" Compute the physical evolution probability using ...

$$
\text { Matched }=\text { Approximate } \frac{\text { Exact }}{\text { Approximate }}
$$

$\rightarrow$ Must be able to compute both numerator and denominator

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$\rightarrow$ Must be able to compute both numerator and denominator and ME corrections,
and by POWHEG for virtual ones

Also similar to GenEva?

Unitarity $\rightarrow$ No need to impose "matching scale" (Matching corrections applied directly to Markov chain as it evolves
$\rightarrow$ self-regulating $\rightarrow$ can be applied over all of phase space, also inside jets)

## pQCD with Markov Chains

Starting Point: reformulate perturbative series as Markov Chain
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Cover all of phase space with (large) trial overestimate = "approximate"
Compute the physical evolution probability using ...

$\rightarrow$ Must be able to compute both numerator and denominator

> | Already widely |
| :---: |
| used at first order: |
| E.g., by PYTHIA for mass |
| and ME corrections, |
| and by POWHEG for |
| virtual ones |
| Also similar to GenEva? |

[^0]
## The Denominator

## Number of Histories:

Existing parton showers are not really Markov Chains
Further evolution (restart scale) depends on which branching happened last $\rightarrow$ proliferation of terms

Number of histories contributing to $\mathbf{n}^{\text {th }}$ branching $\propto \mathbf{2}^{\mathbf{n}} \mathbf{n}$ !

$$
\begin{aligned}
& E \sim K+K+K+K K \begin{array}{|c}
\substack{i=2 \\
\rightarrow 4 \text { terms }}
\end{array} \\
& (N \sim M+K) \substack{\begin{subarray}{c}{i=1 \\
\rightarrow 2 \text { terms }} }} \end{subarray} \substack{ \\
\hline}
\end{aligned}
$$

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\hline}} \\
& \text { Parton- or Catani-Seymour Shower: } \\
& \text { After } 2 \text { branchings: } 8 \text { terms } \\
& \text { After } 3 \text { branchings: } 48 \text { terms } \\
& \text { After } 4 \text { branchings: } 384 \text { terms }
\end{aligned}
$$

## Matched Markovian Antenna Showers

Parton and CS showers: $\mathbf{2}^{\mathbf{n}} \mathbf{n}$ ! One term per parton (two for gluons)

Antenna showers: $\mathbf{2}^{\mathrm{n}} \mathrm{n}!\rightarrow \mathbf{n !}$
One term per parton pair


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+ Change "shower restart" to Markov criterion:
Given an n-parton configuration, "ordering" scale is

$$
Q_{\text {ord }}=\min \left(Q_{E I}, Q_{E 2}, \ldots, Q_{E n}\right)
$$

Unique restart scale, independently of how it was produced


+ Matching: $\mathbf{n !} \rightarrow \mathbf{n}$
Given an $n$-parton configuration, its phase space weight is: $\left|M_{n}\right|^{2}$ : Unique weight, independently of how it was produced


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Matched Markovian Antenna Shower:
After 2 branchings: 2 terms After 3 branchings: 3 terms After 4 branchings: 4 terms

Parton- or Catani-Seymour Shower: After 2 branchings: 8 terms After 3 branchings: 48 terms After 4 branchings: 384 terms

## Approximations

## Distribution of Logio(PSLo/MELo) (inverse ~ matching coefficient)



## Better Approximations

## Distribution of Logio(PSLo/MELo) (inverse ~ matching coefficient)




GEEKS (Giele, Kosower, Skands): arXiv:1102.2126

## + Matching (+ full colour)




GEEKS (Giele, Kosower, Skands): arXiv:1102.2126

## (Speed)

| Matched through: | $\mathrm{Z} \rightarrow 3$ | $Z \rightarrow 4$ | $Z \rightarrow 5$ | $Z \rightarrow 6$ |
| :---: | :---: | :---: | :---: | :---: |
| Pythia 6 <br> (initialization time = zero) <br> Pythia 8 <br> (initialization time = zero) | 0.19 0.20 | ms/event <br> $\mathrm{Z} \rightarrow \mathrm{qq}+$ shower. Matched and unweighted. Hadronization off gfortran/g++ with gcc v.4.4-O2 on single 3.06 GHz processor with 4GB memory gorrtang++ with gcc v.4.4-O2 on single 3.06 GHz processor with 4GB memory |  |  |
| Vincia <br> (initialization time $=$ zero) | 0.24 | 0.62 | 5.60 | 112.50 |
| Sherpa $\left(Q_{\text {macth }}=5 \mathrm{GeV}\right)$ <br> * + intitialization time | $\begin{gathered} 5.15^{*} \\ 90,000 \mathrm{~ms} \end{gathered}$ | $\begin{aligned} & 53.00^{*} \\ & 420,000 \mathrm{~ms} \end{aligned}$ | $220.00^{*}$ <br> $1,320,000 \mathrm{~ms}$ | $\begin{gathered} 400.00^{*} \\ 7,920,000 \mathrm{~ms} \end{gathered}$ |

Generator Versions: Pythia 6.425 (with Perugia 201 I tune), Pythia 8.150, Sherpa I.3.0 ('not including initialization), Vincia I. 026 (NLL,NLC, and uncertainties OFF)
(+ working with J. Lopez-Villarejo at CERN to further increase multi-parton matching speed)

# Uncertainties 

## Uncertainty Variations

## A result is only as good as its uncertainty

Normal procedure:
Run MC $2 \mathrm{~N}+I$ times (for central +N up/down variations)
Takes $2 \mathrm{~N}+1$ times as long

+ uncorrelated statistical fluctuations


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+ uncorrelated statistical fluctuations


## Automate and do everything in one run

VINCIA: all events have weight $=1$
GEEKS (Giele, Kosower, Skands): arXiv:1102.2126
Compute unitary alternative weights on the fly
$\rightarrow$ sets of alternative weights representing variations (all with $\langle w\rangle=1$ ) Same events, so only have to be hadronized/detector-simulated ONCE!

## MC with Automatic Uncertainty Bands

## Uncertainties

For each branching, recompute weight for:

- Different renormalization scales
- Different antenna functions
- Different ordering criteria
- Different subleading-colour treatments

|  | Weight |
| :--- | :---: |
| Nominal | I |
| Variation | $P_{2}=\frac{\alpha_{s 2} a_{2}}{\alpha_{s 1} a_{1}} P_{1}$ |

## Uncertainties

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## + Unitarity

For each failed branching:

$$
P_{2 ; \mathrm{no}}=1-P_{2}=1-\frac{\alpha_{s 2} a_{2}}{\alpha_{s 1} a_{1}} P_{1}
$$

## Uncertainties

## For each branching, recompute weight for:

- Different renormalization scales
- Different antenna functions
- Different ordering criteria
- Different subleading-colour treatments
+ Matching
Differences explicitly matched out
(Up to matched orders)
(Can in principle also include variations of matching scheme...)

|  | Weight |
| :--- | :---: |
| Nominal | I |
| Variation | $P_{2}=\frac{\alpha_{s 2} a_{2}}{\alpha_{s 1} a_{1}} P_{1}$ |

## + Unitarity

For each failed branching:

$$
P_{2 ; \mathrm{no}}=1-P_{2}=1-\frac{\alpha_{s 2} a_{2}}{\alpha_{s 1} a_{1}} P_{1}
$$

## Automatic Uncertainties

## Vincia:uncertaintyBands = on



Variation of renormalization scale (no matching)

## Automatic Uncertainties

## Vincia:uncertaintyBands = on



Variation of "finite terms" (no matching)

## Putting it Together

VinciaMatching:order $=0$
VinciaMatching:order $=3$




## VINCIA STATUS

PLUG-IN TO PYTHIA 8
STABLE AND RELIABLE FOR FINALSTATE JETS (E.g. lep)

AUTOMATIC MATCHING AND UNCERTAINTY BANDS

IMPROVEMENTS IN SHOWER (SMOOTH ORDERING, NLC, MATCHING, ...)
PAPER ON MASS EFFECTS~READY
(WITH A. GEHRMANN-DE-RIDDER \& M. RITZMANN)

## NEXT STEPS

MULTI-LEG ONE-LOOP MATCHING
(WITH L. HARTGRING \& E. LAENEN, NIKHEF)

## "SECTOR SHOWERS"

(WITH J. LOPEZ-VILLAREJO, CERN)

## $\rightarrow$ INITIAL-STATE SHOWERS

(WITH W. GIELE, D. KOSOWER)

## VINCIA STATUS

# stroter 

\#1 GUEST RATED SHOWERHEAD - ALL NEW

## NEXT STEPS

MULTI-LEG ONE-LOOP MATCHING
(WITH L. HARTGRING \& E. LAENEN, NIKHEF)
"SECTOR SHOWERS"
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$\rightarrow$ INITIAL-STATE SHOWERS
(WITH W. GIele, D. Kosower)
HTTP://PROJECTS.HEPFORGE.ORG/VINCIA


## pQCD as Markov Chain

## Start from Born Level:



## pQCD as Markov Chain

## Start from Born Level:



## Insert Evolution Operator, S:



$$
\left.\frac{\mathrm{d} \sigma_{H}}{\mathrm{~d} \mathcal{O}}\right|_{\mathcal{S}}=\int \mathrm{d} \Phi_{H}\left|M_{H}^{(0)}\right|^{2} \mathcal{S}\left(\{p\}_{H}, \mathcal{O}\right)
$$

Think: starting a shower off an incoming on-shell momentum configuration Postpone evaluating observable until shower "finished"

## The Evolution Operator

## Depends on Evolution Scale : $\mathbf{Q E}_{\mathbf{E}}$

$$
\mathcal{S}\left(\{p\}_{H}, s, Q_{E}^{2}, \mathcal{O}\right)=\underbrace{\Delta^{\kappa}\left(\{p\}_{H}, s, Q_{E}^{2}\right) \delta\left(\mathcal{O}-\mathcal{O}\left(\{p\}_{H}\right)\right)}_{H+0 \text { exclusive above } Q_{E}}
$$


$H+1$ inclusive above $Q_{E}$

## Legend:

$\Delta$ represents no-evolution probability (Sudakov): conserves probability = preserves event weights

## The Evolution Operator

## Depends on Evolution Scale : $\mathbf{Q E}_{\mathbf{E}}$

$$
\mathcal{S}\left(\{p\}_{H}, s, Q_{E}^{2}, \mathcal{O}\right)=\underbrace{\Delta^{*}\left(\{p\}_{H}, s, Q_{E}^{2}\right) \delta\left(\mathcal{O}-\mathcal{O}\left(\{p\}_{H}\right)\right)}_{H+0 \text { exclusive above } Q_{E}}
$$



## Legend:

$\Delta$ represents no-evolution probability (Sudakov): conserves probability = preserves event weights
$S_{r}=$ Emission probability (partitioned among radiators r)
According to best known approximation to $\left|H+| |^{2}\right.$ (e.g., ME or LL shower)

## (Expand S to First Order)

## Equivalent to Sjöstrand/POWHEG

$$
\mathcal{S}^{(1)}\left(\{p\}_{H}, s, Q_{E}^{2}, \mathcal{O}\right)=\left(1+K_{H}^{(1)}-\int_{Q_{E}^{2}}^{s} \frac{\mathrm{~d} \Phi_{H+1}}{\mathrm{~d} \Phi_{H}} \frac{\left|M_{H+1}^{(0)}\right|^{2}}{\left|M_{H}^{(0)}\right|^{2}}\right)
$$



$$
+\int_{Q_{E}^{2}}^{s} \frac{\mathrm{~d} \Phi_{H+1}}{\mathrm{~d} \Phi_{H}} \frac{\left|M_{H+1}^{(0)}\right|^{2}}{\left|M_{H}^{(0)}\right|^{2}} \delta\left(\mathcal{O}-\mathcal{O}\left(\{p\}_{H+1}\right)\right)
$$

## (Expand S to First Order)

## Equivalent to Sjöstrand/POWHEG

$$
\begin{aligned}
& \mathcal{S}^{(1)}\left(\{p\}_{H}, s, Q_{E}^{2}, \mathcal{O}\right)=\left(1+K_{H}^{(1)}\right.\left.-\int_{Q_{E}^{2}}^{s} \frac{\text { "NLO" virtual correction }}{\mathrm{d} \Phi_{H+1}} \frac{\left|M_{H+1}^{(0)}\right|^{2}}{\left|M_{H}^{(0)}\right|^{2}}\right) \delta\left(\mathcal{O}-\mathcal{O}\left(\{p\}_{H}\right)\right) \\
& \uparrow \text { Unitarity }
\end{aligned}
$$

Virtual Correction (NLO normalization)

$$
\underbrace{\frac{2 \operatorname{Re}\left[M_{H}^{(0)} M_{H}^{(1) *}\right]}{\left|M_{H}^{(0)}\right|^{2}}}_{\frac{a}{\epsilon^{2}}+\frac{b}{\epsilon}+c+\mathcal{O}(\epsilon)}=K_{c^{-}}^{\substack{(1)}}-\underbrace{\int_{0}^{s} \frac{\mathrm{~d} \Phi_{H+1}}{\mathrm{~d} \Phi_{H}} \frac{\left|M_{H+1}^{(0)}\right|^{2}}{\left|M_{H}^{(0)}\right|^{2}}}_{\frac{a}{\epsilon^{2}}+\frac{b}{\epsilon}+c^{\prime}+\mathcal{O}(\epsilon)}
$$

## Simple Solution

## Generate Trials without imposing strong ordering

At each step, each dipole allowed to fill its entire phase space
Overcounting removed by matching (revert to strong ordering beyond matched multiplicities)



## Better Solution

## Generate Trials without imposing strong ordering

At each step, each dipole allowed to fill its entire phase space Overcounting removed by matching

+ smooth ordering beyond matched multiplicities

$$
\frac{\hat{p}_{\perp}^{2}}{\hat{p}_{\perp}^{2}+p_{\perp}^{2}} P_{\mathrm{LL}} \quad \begin{array}{lll}
\hat{p}_{\perp}^{2} & \text { last branching } \\
p_{\perp}^{2} & \text { current branching }
\end{array}
$$




## (Subleading Singularities)

## Isolate double-collinear region:



## LEP event shapes





## PYTHIA 8 already doing a very good job

## VINCIA adds uncertainty bands + can look at more exclusive observables?

## Multijet resolution scales




## 4-Jet Angles

## 4-jet angles

## Sensitive to

 polarization effects
## Good News

VINCIA is doing reliably well
Non-trivial verification that shower+matching is working, etc.

## Higher-order matching needed?

PYTHIA 8 already doing a very good job on these observables





Interesting to look at more exclusive observables, but which ones?


[^0]:    Unitarity $\rightarrow$ No need to impose "matching scale" (Matching corrections applied directly to Markov chain as it evolves
    $\rightarrow$ self-regulating $\rightarrow$ can be applied over all of phase space, also inside jets)
    $\rightarrow$ One single unweighted event sample (Effectively, n-parton samples use parton shower itself as phase space generator $=$ highly efficient "multi-channel" integration $\rightarrow$ speed gains expected, + unitarity $\rightarrow$ unit-weights)

